

**SOME FEATURES OF ELECTRICAL TRANSPORT IN
NONLINEAR INHOMOGENEOUS SYSTEMS**

**THESIS SUBMITTED FOR THE DEGREE OF
DOCTOR OF PHILOSOPHY (SCIENCE)
OF THE
UNIVERSITY OF CALCUTTA**

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INDIA

1999

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