

# APPENDIX C

## Index

- \* Capitalization has been disregarded in the alphabetization of the index. Word boundaries, even those involving hyphens and apostrophes, have also been disregarded.
- \* All diacritical marks have also been ignored in the alphabetization. Thus, *Möbius* appears at the place where *Mobius* would have appeared.
- \* A mark of ‘•’ after an entry signifies that, for that particular entry, we have only given page reference to the place where it was first introduced or was discussed in some detail. There are too many appearances of any such entry to record each of them.

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